

# Band Energy Dependence of Defect Formation in the Topological Semimetal $\text{Cd}_3\text{As}_2$

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**Session Y44: Dirac and Weyl Semimetal: Theory**

**APS March Meeting 2023**

**Las Vegas, Nevada**

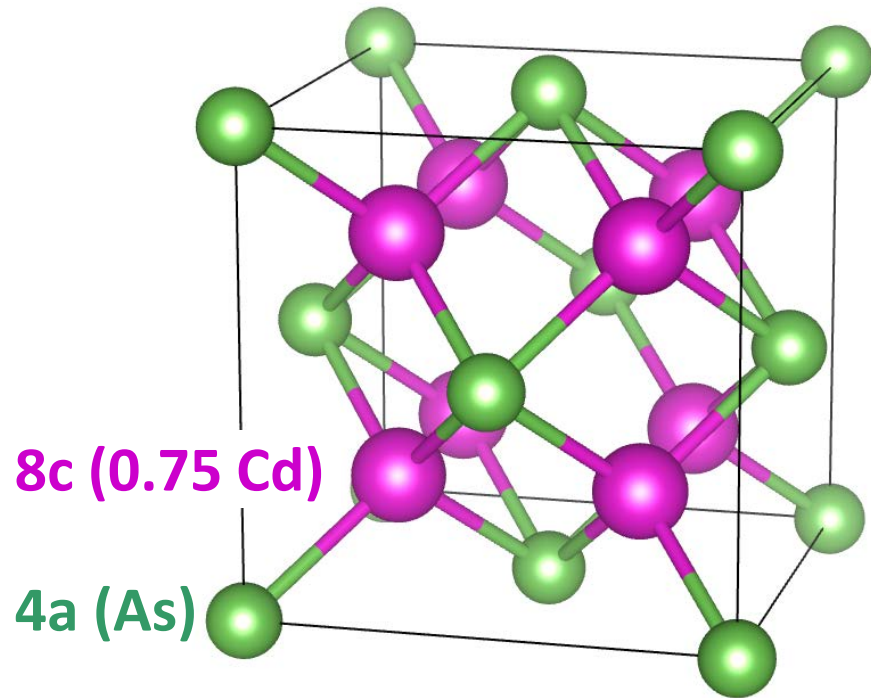
# Cd<sub>3</sub>As<sub>2</sub> structure

## Fluorite structure (sg 225)

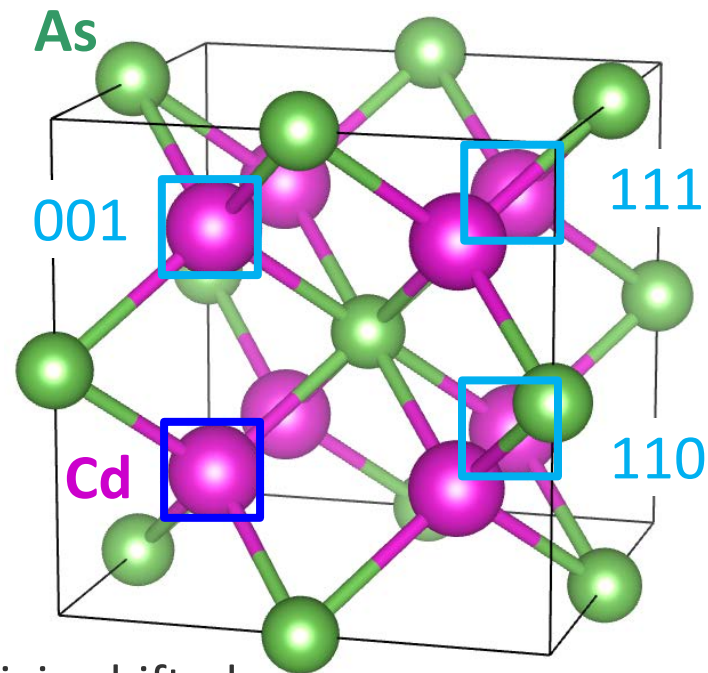


Conventional cell: 12 atom (sc)

Primitive cell: 3 atom (fcc)

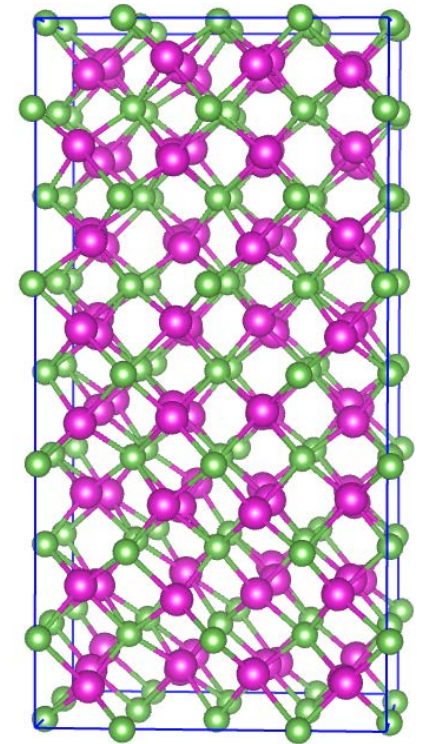


2 empty sites per sc cell  
for Cd<sub>3</sub>As<sub>2</sub> stoichiometry



origin shifted  
by (0.5, 0.5, 0.5)

ground state  
sg 142, centrosymmetric  
no spin splitting  
80 atom primitive cell



Ali *et al*, Inorg Chem  
53, 4062 (2014)

# Unintentional $n$ -doping in $\text{Cd}_3\text{As}_2$

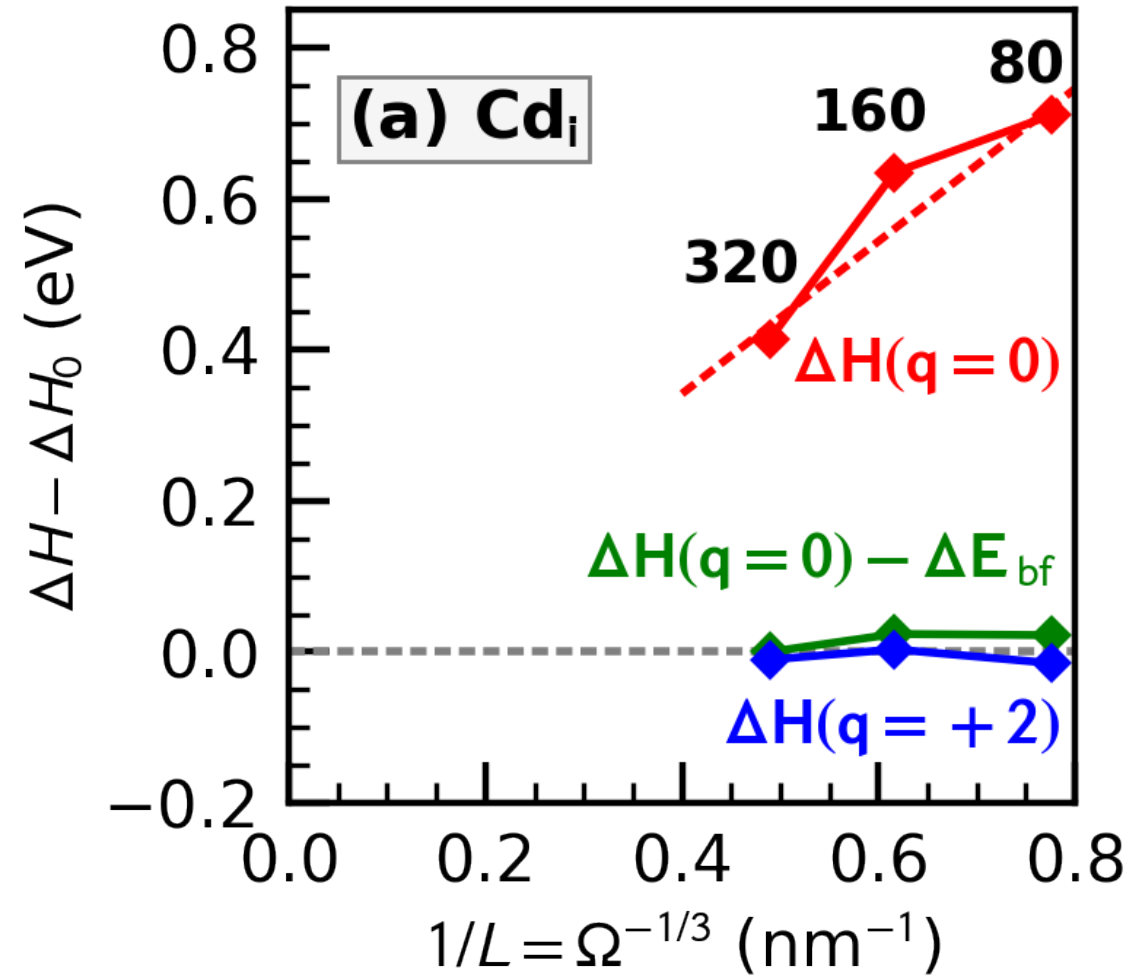
## First principles defect calculations

- Cd interstitial on empty site
- Cell size dependence  
80 to 320 atoms
- DFT-PBE functional (vasp)
- DFT-SCAN + spin-orbit
- QSGW electronic structure (questaal)

## Defect formation energy

- Charged states in semiconductors
- In metals usually only neutral ( $q=0$ )

$$\Delta H_{D,q}(E_F, \{\mu\}) = [E_{D,q} - E_h] + \sum_{\alpha} n_{\alpha} \mu_{\alpha} + qE_F$$

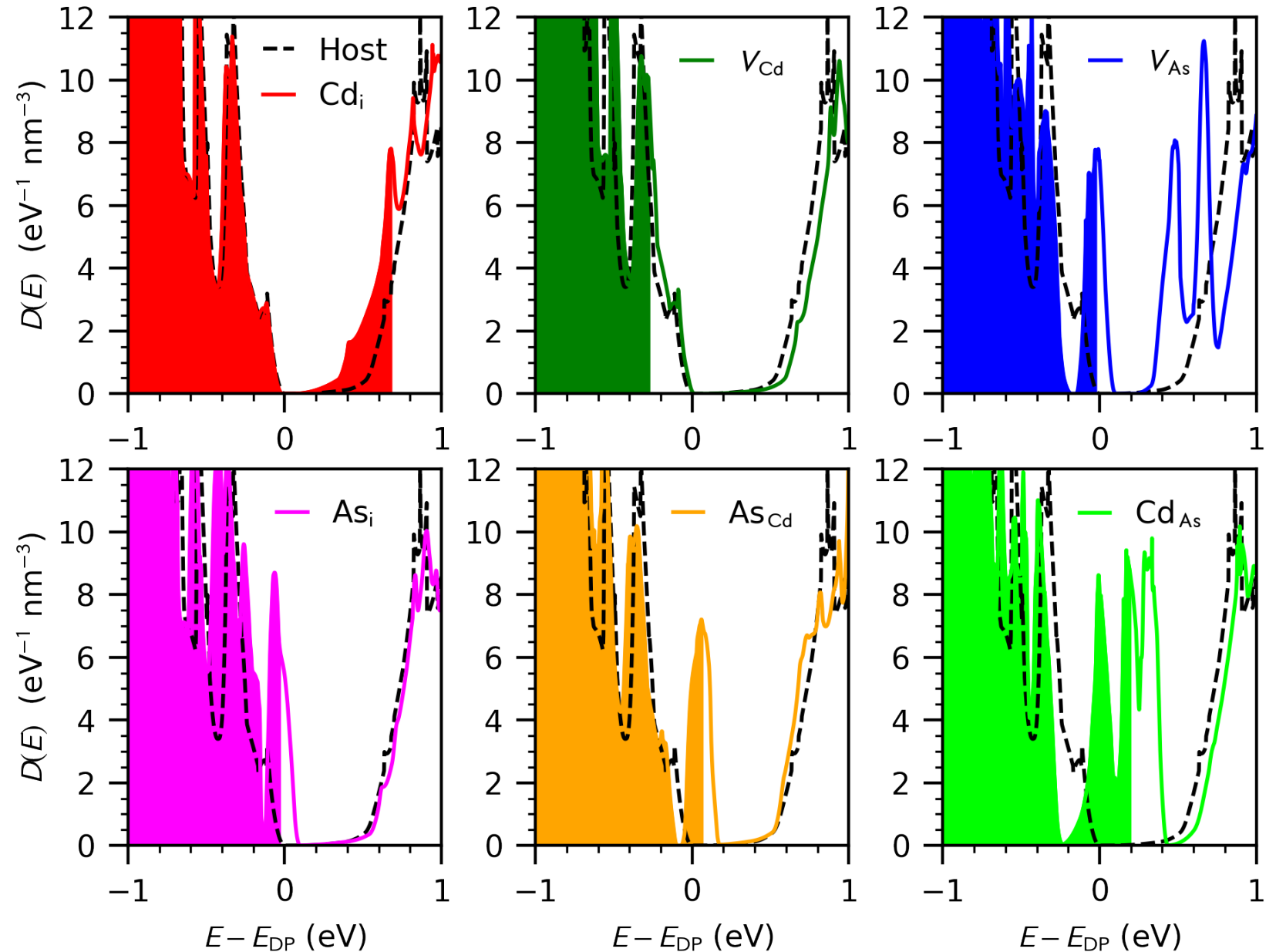


Brooks *et al*, under review

# DOS

## Defect behavior

- Defect state vs band continuum
- $\text{Cd}_i$  donors
- $V_{\text{Cd}}$  acceptor
- $V_{\text{As}}$  amphoteric

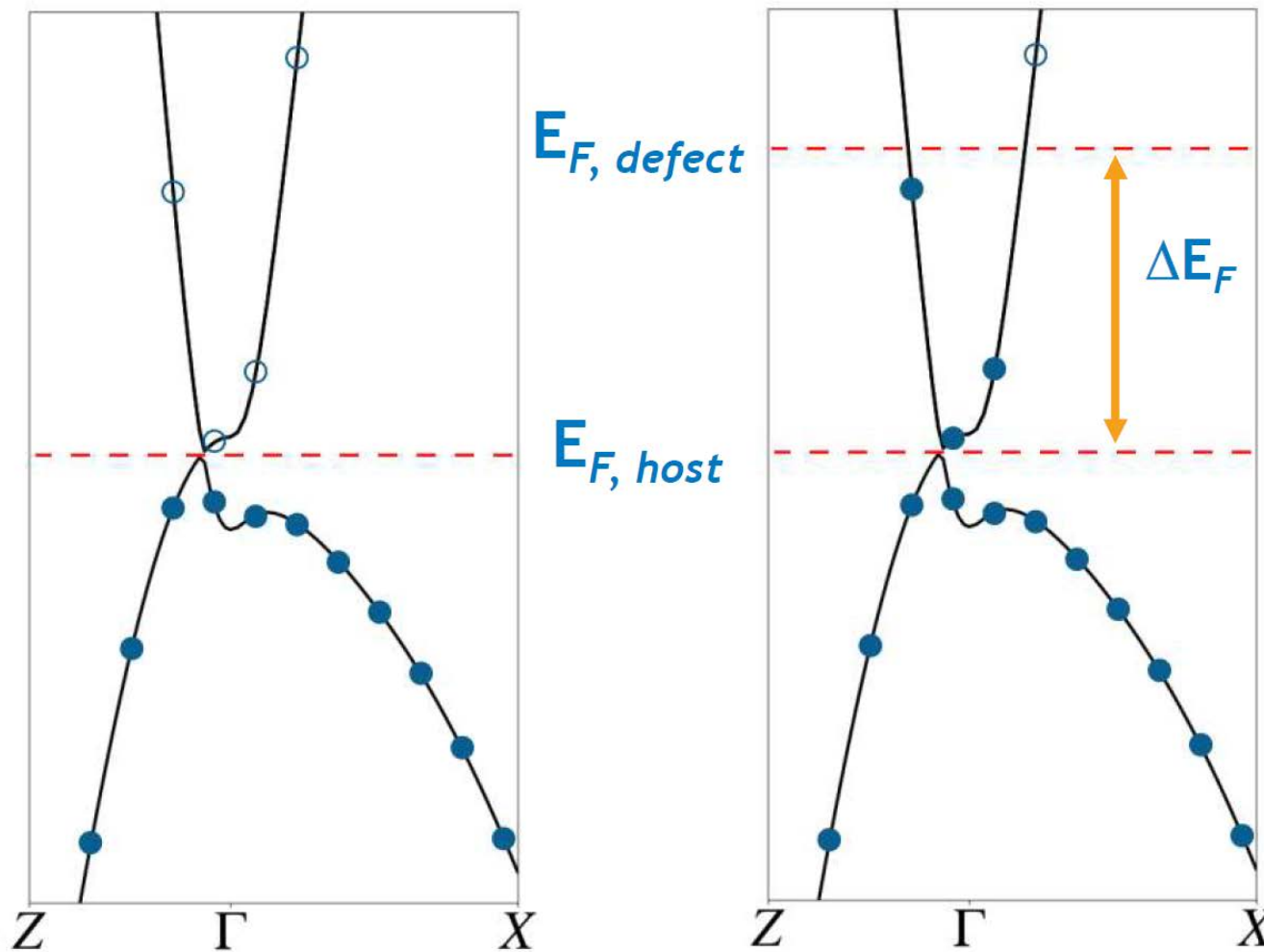
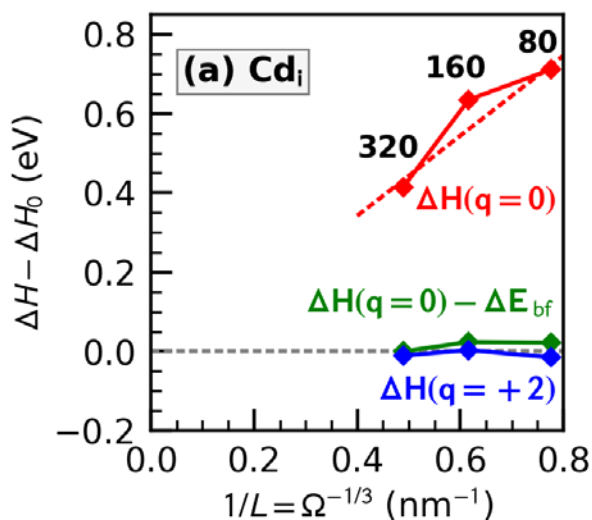


# Origin of cell size dependence of $\Delta H_D$

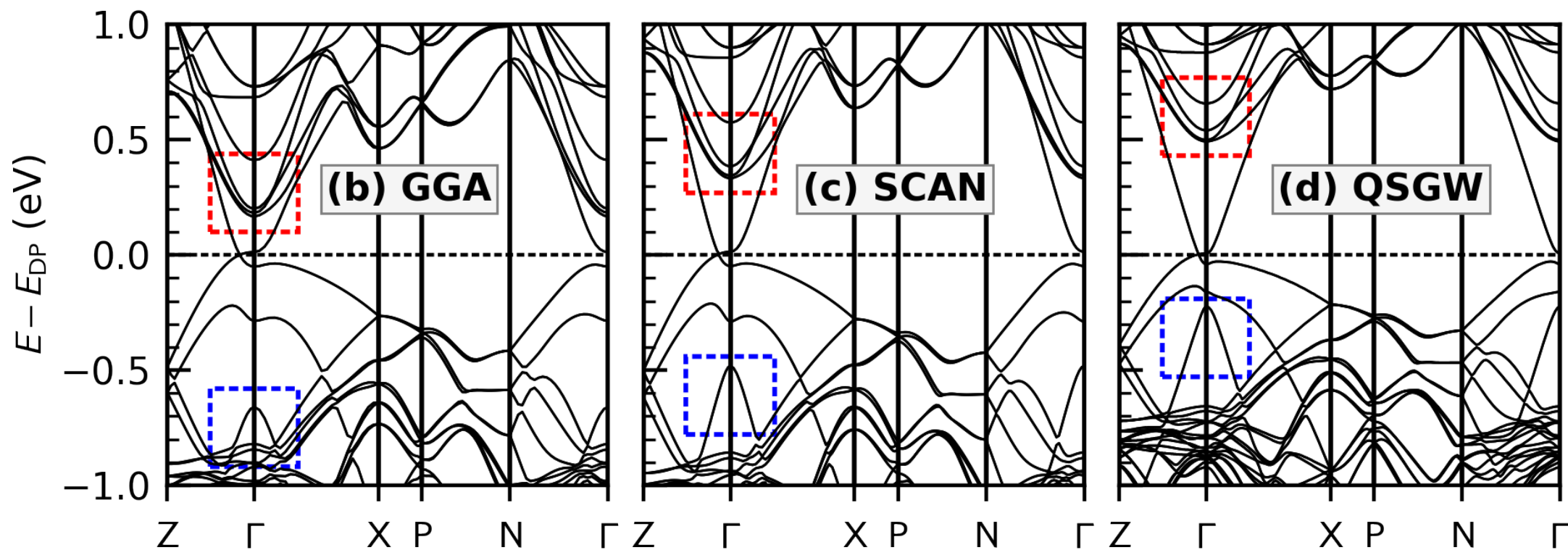
$$\Delta E_{bf} = \sum_{\substack{n, \mathbf{k} \\ \varepsilon_{n, \mathbf{k}} > E_{DP}}} w_{\mathbf{k}} f_{n, \mathbf{k}} (\varepsilon_{n, \mathbf{k}} - E_{DP})$$

## Band filling energies

- Dopant donates electrons
- Concentration dependence
- BF energy recovers charged defect  $\Delta H_D$
- $\text{Cd}_i^0$  better described as  $\text{Cd}_i^{2+} + 2e$

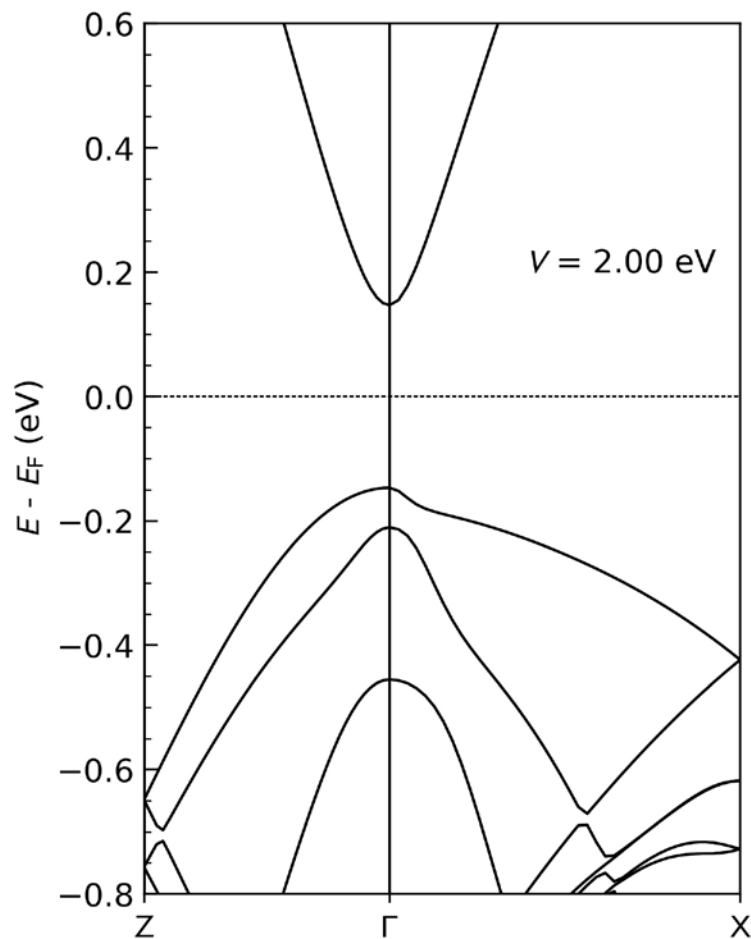


# Electronic structure: Level of theory



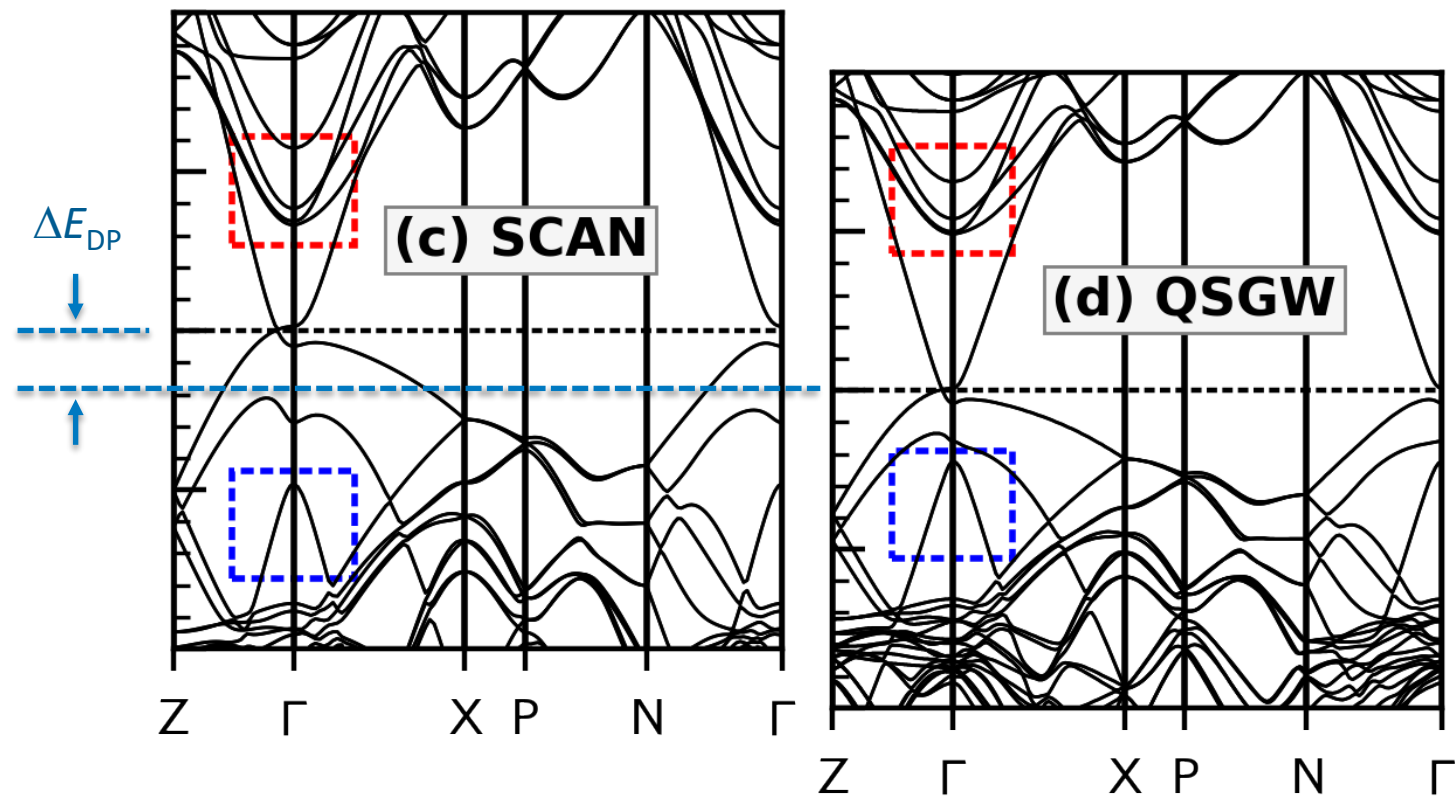
- SCAN lies halfway between standard DFT (GGA) and QSGW
- Upward shift of s-like Cd and As states, analogous to semiconductors
- Offset  $\Delta E_{\text{DP}} -0.19$  eV on absolute energy scale

# Electronic structure: Band inversion and absolute energy scale



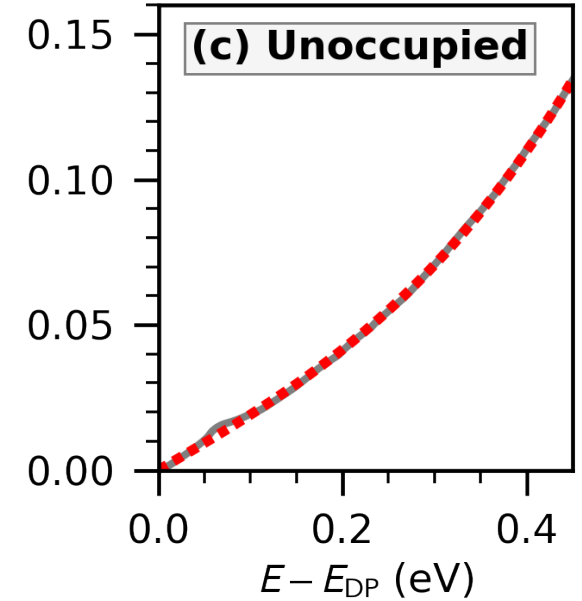
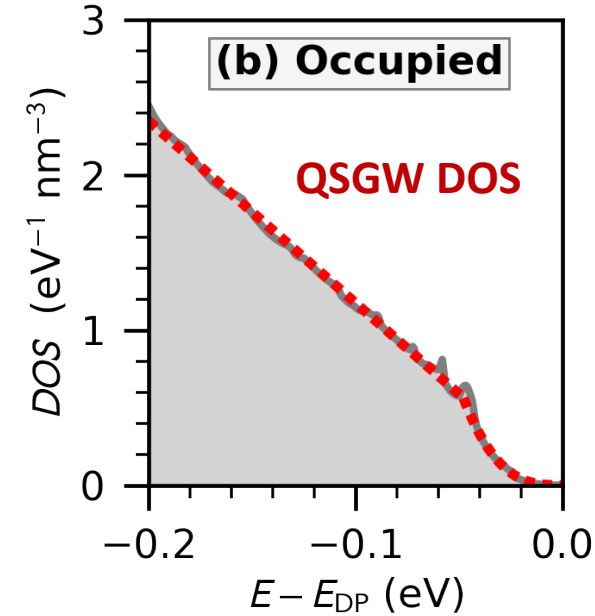
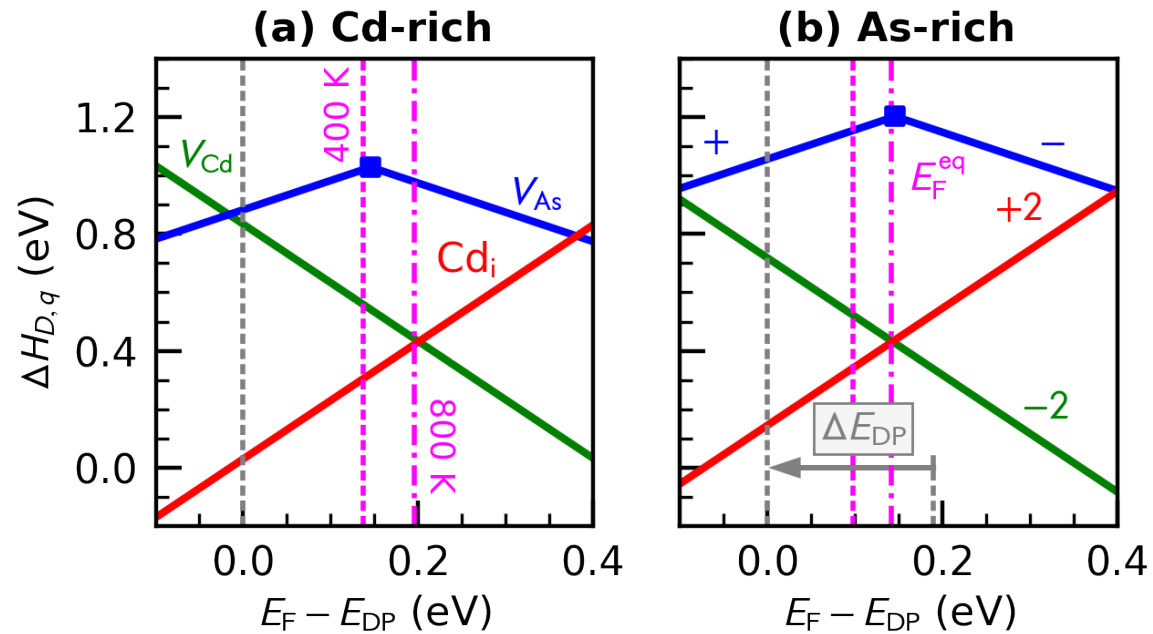
Cd-s and As-s onsite potential

$$\hat{V} = \sum_{i,j} |p_i\rangle \langle \phi_i^{\text{AE}} | V_s | \phi_j^{\text{AE}} \rangle \langle p_j |$$



Offset  $\Delta E_{\text{DP}} -0.19$  eV on absolute energy scale

# Defect equilibria



- $Cd_i$  and  $V_{Cd}$  are dominant defect, difference determines doping
- Defect equilibrium with charge balance (defects and carriers)

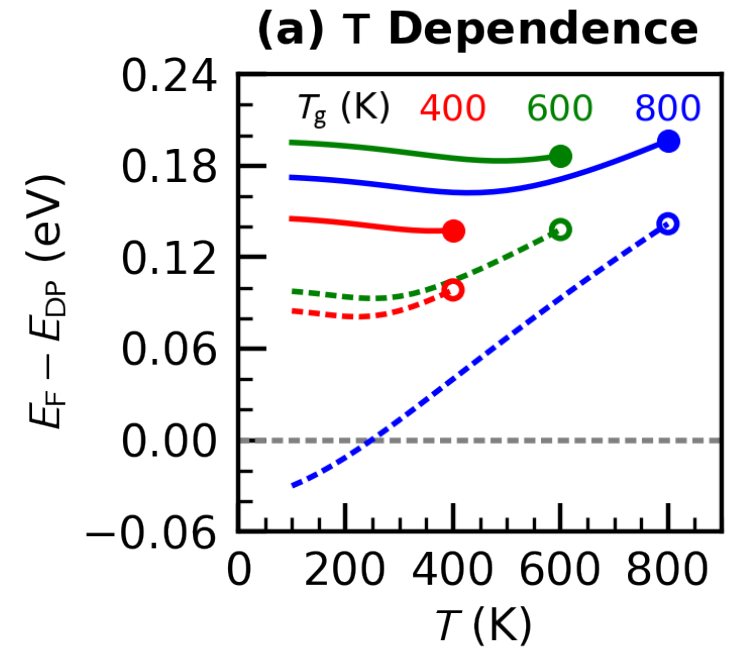
$$c_{D,q}(E_F, \{\mu\}, T) = N_D e^{-\Delta H_{D,q}(E_F, \{\mu\})/k_B T}$$

$$n_e = \int_{E_{DP}}^{\infty} \frac{g_{QSGW}(E)}{e^{(E-E_F)/k_B T} + 1} dE$$

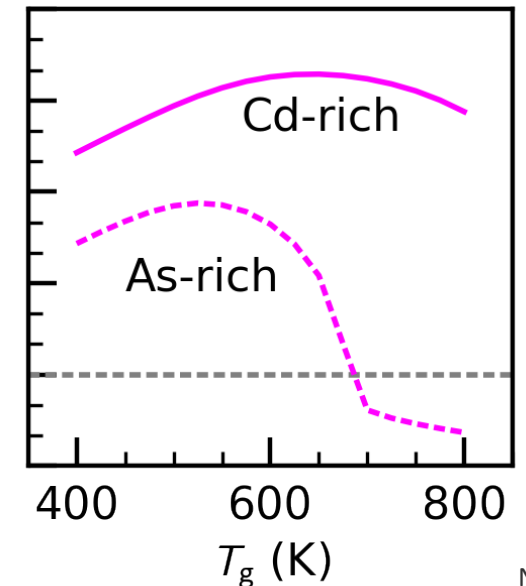
# Doping type inversion

Cd/As rich	$T_g$ (K)	$Cd_i$	$c_D$ ( $cm^{-3}$ ) $V_{Cd}$	$V_{As}$	$c_{nd}$ ( $cm^{-3}$ )
Cd	400	$1.0 \times 10^{18}$	$8.2 \times 10^{14}$	$1.3 \times 10^9$	$2.0 \times 10^{18}$
	600	$3.0 \times 10^{18}$	$1.2 \times 10^{18}$	$3.0 \times 10^{13}$	$3.7 \times 10^{18}$
	800	$1.6 \times 10^{19}$	$1.5 \times 10^{19}$	$4.6 \times 10^{15}$	$2.9 \times 10^{18}$
As	400	$3.5 \times 10^{17}$	$2.4 \times 10^{15}$	$2.2 \times 10^7$	$6.9 \times 10^{17}$
	600	$2.1 \times 10^{18}$	$1.7 \times 10^{18}$	$1.0 \times 10^{12}$	$9.1 \times 10^{17}$
	800	$1.5 \times 10^{19}$	$1.6 \times 10^{19}$	$3.6 \times 10^{14}$	$-2.7 \times 10^{18}$

- Non-monotonic temperature dependence of  $E_F$
- Doping inversion from  $n$ - to  $p$ -type (As-rich high  $T_g$ )



**(b)  $T \rightarrow 0$  Limit**



Brooks *et al*, (2023, under review)

# Thank you

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NREL/PR-5K00-85538

This work was performed in part at the National Renewable Energy Laboratory, operated by Alliance for Sustainable Energy, LLC, for the U.S. Department of Energy (DOE) under Contract No. DE-AC36-08GO28308. Funding provided by the U.S. Department of Energy, Office of Science, Basic Energy Sciences, Physical Behavior of Materials Program. The views expressed in the article do not necessarily represent the views of the DOE or the U.S. Government. The U.S. Government retains and the publisher, by accepting the article for publication, acknowledges that the U.S. Government retains a nonexclusive, paid-up, irrevocable, worldwide license to publish or reproduce the published form of this work, or allow others to do so, for U.S. Government purposes.

